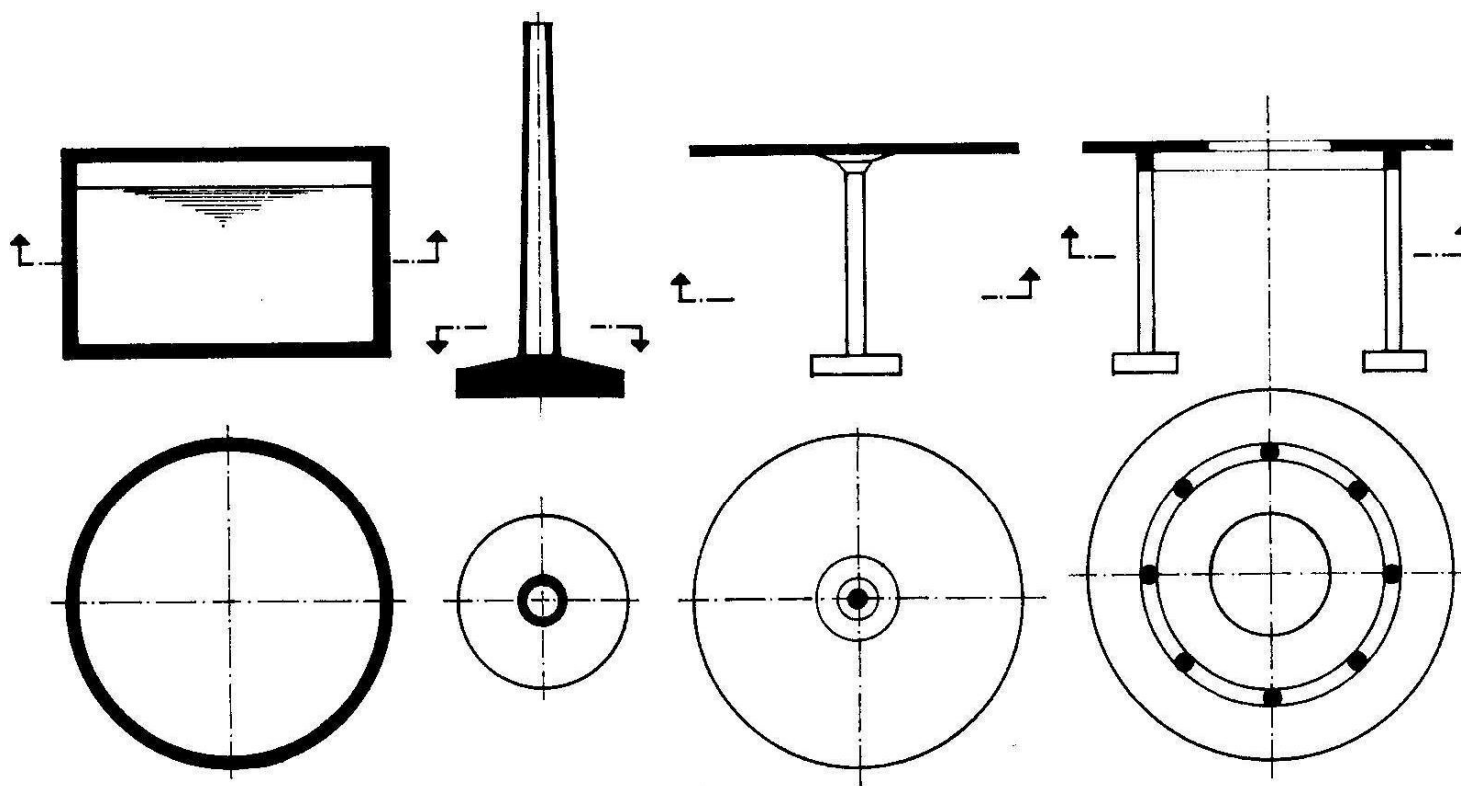


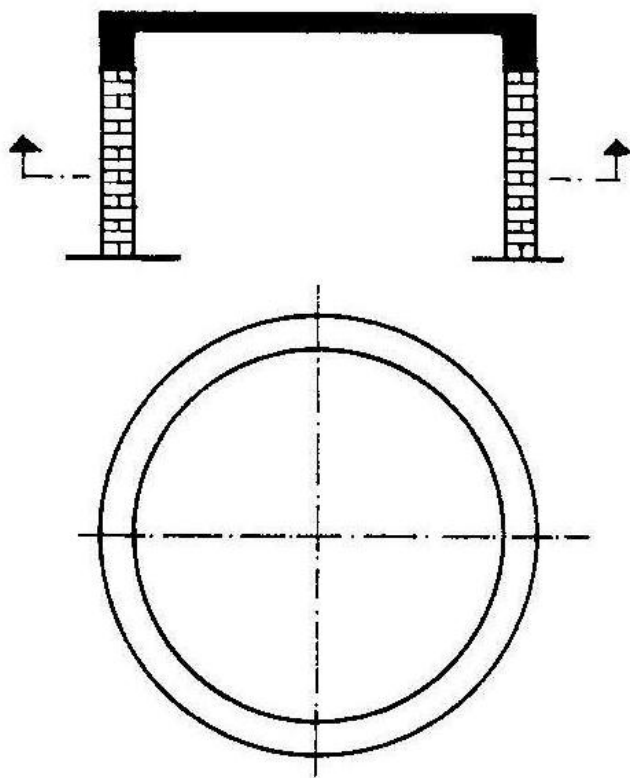
# Kružne i prstenaste armiranobetonske ploče

Kružne ploče mogu biti deo međuspratne konstrukcije, ali se najčešće javljaju kao ploče kružnih nadstrešnica, krovne i temeljne ploče kružnih rezervoara, temeljne ploče dimnjaka, tornjeva i sličnih konstrukcija. Kružne ploče sa većim srednjim otvorom nazivaju se prstenaste ploče.

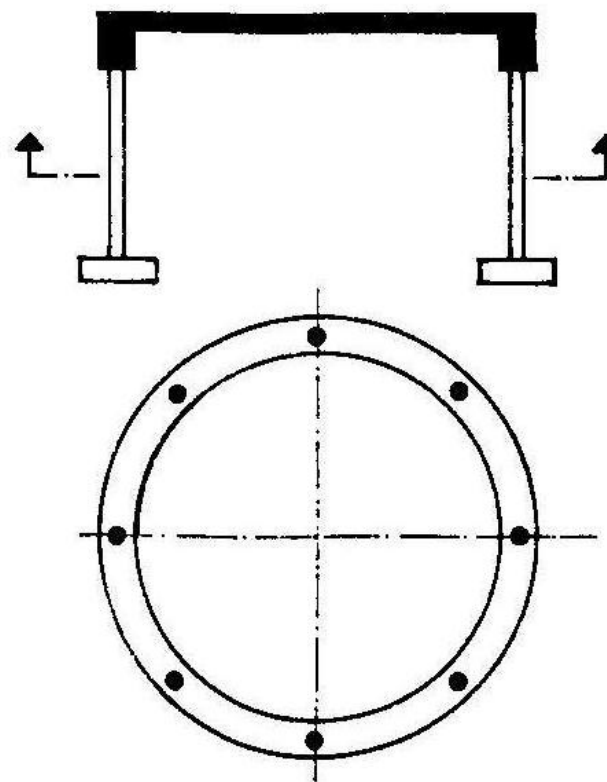


# Načini oslanjanja kružnih ploča

a) Kontinualno oslanjanje na zid  
(od opeke ili armiranobetonski)



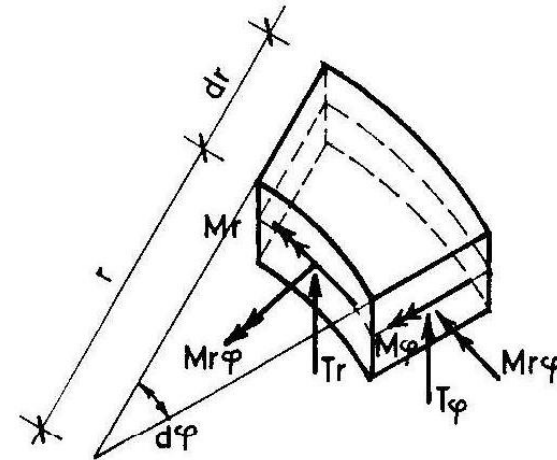
b) oslanjanje na stubove preko  
kružne grede



# Presečne sile u ploči

Za delovanje opterećenja upravno na srednju površ ploče, pri savijanju se javljaju pomeranja u pravcu normale na srednju površ ( $w$ ), kao i pomeranja u radijalnom ( $u$ ) i tangencijalnom ( $v$ ) pravcu. Pomeranja na odstojanju  $z$  od srednje ravni ploče su:

$$w_z = w(r, \phi) \quad , \quad u_z = - \frac{\partial w}{\partial r} z \quad , \quad v_z = - \frac{z}{r} \frac{\partial w}{\partial \phi}$$



Dilatacije u radijalnom i tangencijalnom pravcu i klizanja se mogu izraziti preko ovih pomeranja:

$$\epsilon_r = \frac{\partial u}{\partial r} = - z \frac{\partial^2 w}{\partial r^2} \quad , \quad \epsilon_\phi = \frac{u}{r} + \frac{1}{r} \frac{\partial v}{\partial \phi} = - \frac{z}{r} \frac{\partial w}{\partial r} - \frac{z}{r^2} \frac{\partial^2 w}{\partial \phi^2} \quad , \quad \epsilon_z = 0$$

$$\gamma_{r\phi} = \frac{1}{r} \frac{\partial u}{\partial \phi} + \frac{\partial v}{\partial r} - \frac{v}{r} = - 2z \left( \frac{1}{r} \frac{\partial^2 w}{\partial r \partial \phi} - \frac{1}{r^2} \frac{\partial w}{\partial \phi} \right) \quad , \quad \gamma_{zr} = \gamma_{z\phi} = 0$$

Kada se komponente napona izraze preko komponenti deformacija:

$$\sigma_r = \frac{E}{1-\nu^2} (\epsilon_r + \nu \epsilon_\phi) = \frac{-Ez}{1-\nu^2} \left( \frac{\partial^2 w}{\partial r^2} + \frac{\nu}{r} \frac{\partial w}{\partial \phi} + \frac{\nu}{r^2} \frac{\partial^2 w}{\partial \phi^2} \right)$$

$$\sigma_\phi = \frac{E}{1-\nu^2} (\epsilon_\phi + \nu \epsilon_r) = \frac{-Ez}{1-\nu^2} \left( \frac{1}{r} \frac{\partial w}{\partial r} + \frac{1}{r^2} \frac{\partial^2 w}{\partial \phi^2} + \nu \frac{\partial^2 w}{\partial r^2} \right)$$

$$\tau_{r\phi} = G \gamma_{r\phi} = \frac{-Ez}{(1+\nu)} \left( \frac{1}{r} \frac{\partial^2 w}{\partial r \partial \phi} - \frac{1}{r^2} \frac{\partial w}{\partial \phi} \right),$$

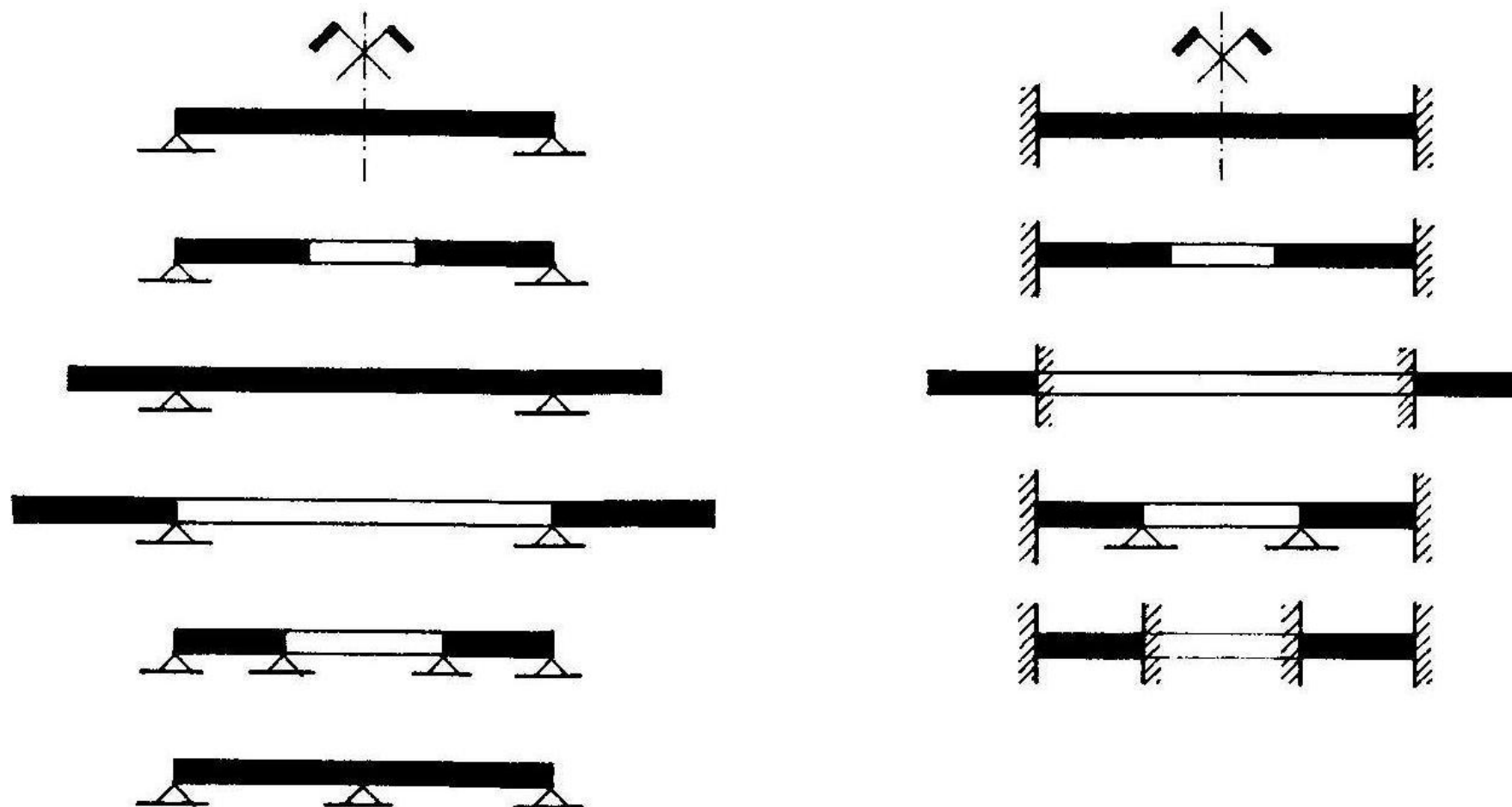
i kada se sile u preseku izraze preko komponenti napona, dobijaju se veze u sledećem obliku:

$$\begin{aligned} M_r &= \int_{-d/2}^{d/2} \sigma_r z dz & M_\phi &= \int_{-d/2}^{d/2} \sigma_\phi z dz & M_{r\phi} &= \int_{-d/2}^{d/2} \tau_{r\phi} z dz \\ T_r &= \int_{-d/2}^{d/2} \tau_{rz} dz & T_\phi &= \int_{-d/2}^{d/2} \tau_{\phi z} dz \end{aligned} \quad ($$

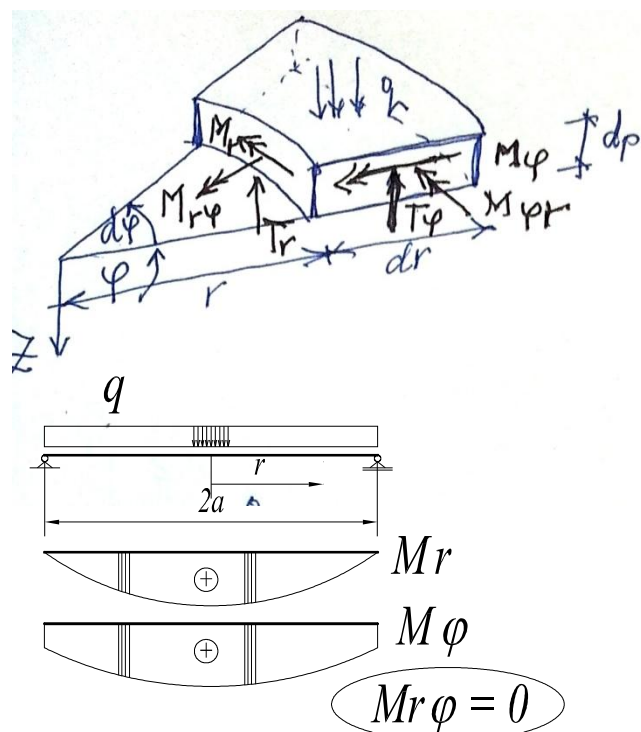
Posle integracije i koristeći veze napona i pomeranja, dobijaju se momenti savijanja i torzije u funkciji ugiba tačaka ploče:

$$\begin{aligned} M_r &= -K \left[ \frac{\partial^2 w}{\partial r^2} + \nu \left( \frac{1}{r^2} \frac{\partial^2 w}{\partial \phi^2} + \frac{1}{r} \frac{\partial w}{\partial r} \right) \right] \\ M_\phi &= -K \left[ \nu \frac{\partial^2 w}{\partial r^2} + \frac{1}{r^2} \frac{\partial^2 w}{\partial \phi^2} + \frac{1}{r} \frac{\partial w}{\partial r} \right] \end{aligned}$$

# Statički sistemi kružnih i prstenastih ploča

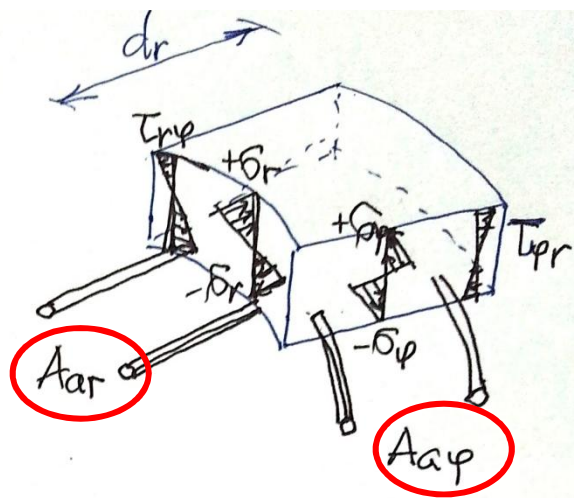


# Statički uticaji i dimenzionisanje

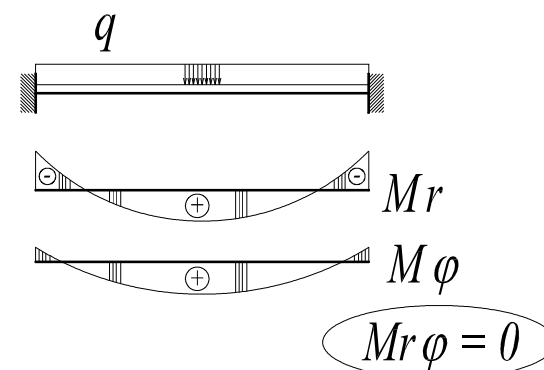


$$M_r = \frac{q \cdot a^2}{16} [(1 - \rho^2)(3 + \nu)]$$

$$M_\varphi = \frac{q \cdot a^2}{16} [(3 + \nu) - \rho^2(1 + 3\nu)]$$



$$\rho = \frac{r}{a}$$

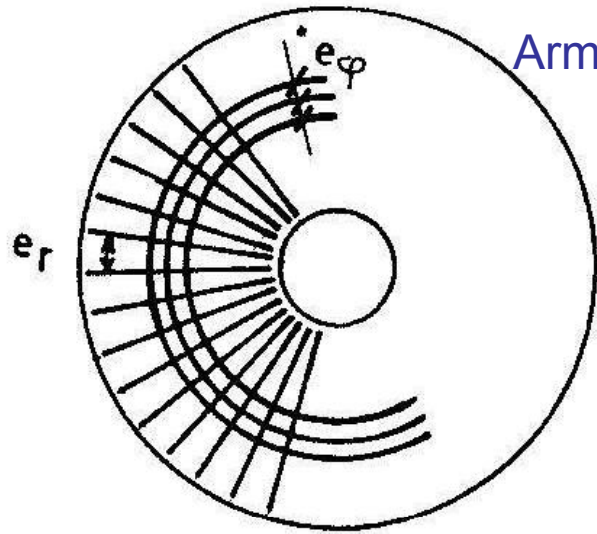


$$M_r = \frac{q \cdot a^2}{16} [(1 + \nu) - (3 + \nu)\rho^2]$$

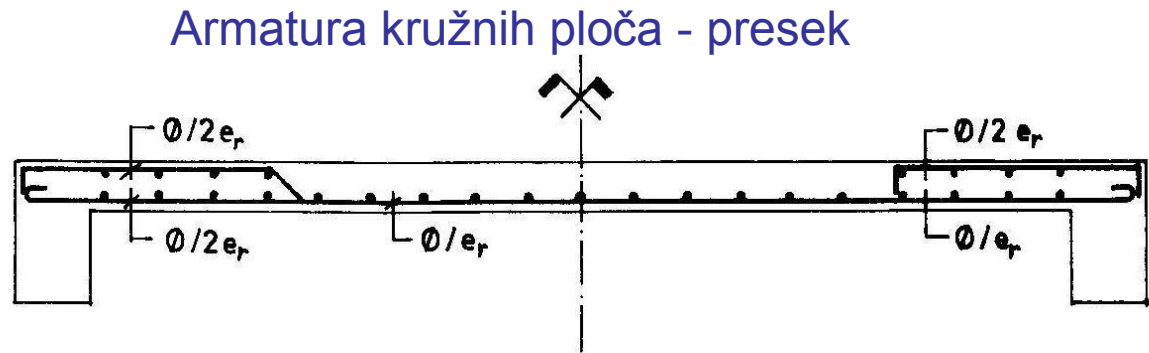
$$M_\varphi = \frac{q \cdot a^2}{16} [(1 + \nu) - (1 + 3\nu)\rho^2]$$

Dimenzionisanje ploče se vrši kao dimenzionisanje pravougaonih preseka na čisto savijanje, dimenzija  $d_p$  i  $b = 100$  cm, prema radijalnim i tangencijalnim momentima savijanja, a pri tome je:  $h_x \neq h_y$

# Armiranje kružnih i prstenastih ploča



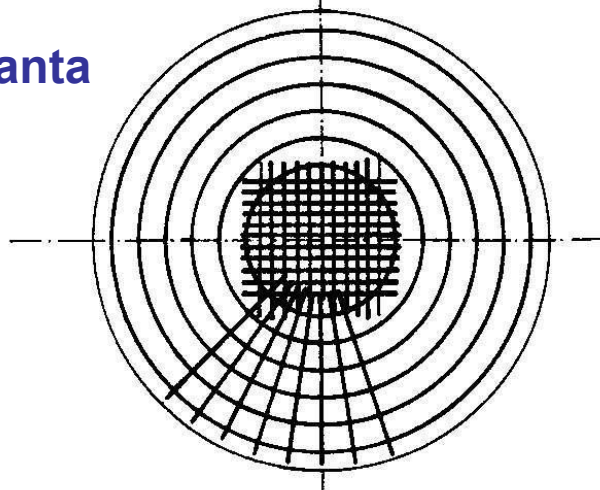
Armatura prstenaste ploče – osnova



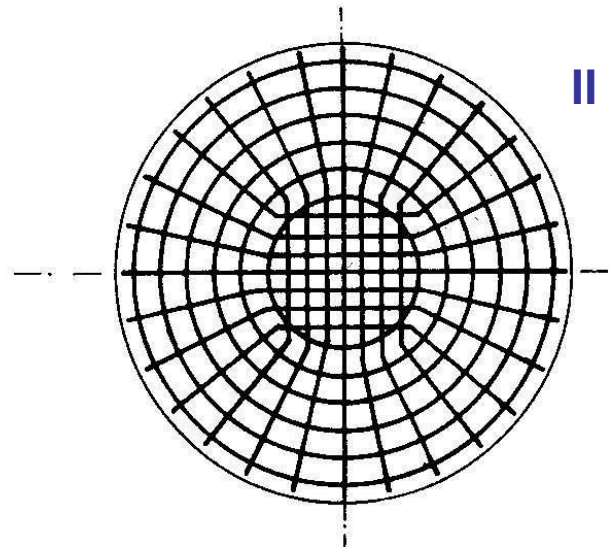
Armatura kružnih ploča - presek

Armatura kružnih ploča – osnova:

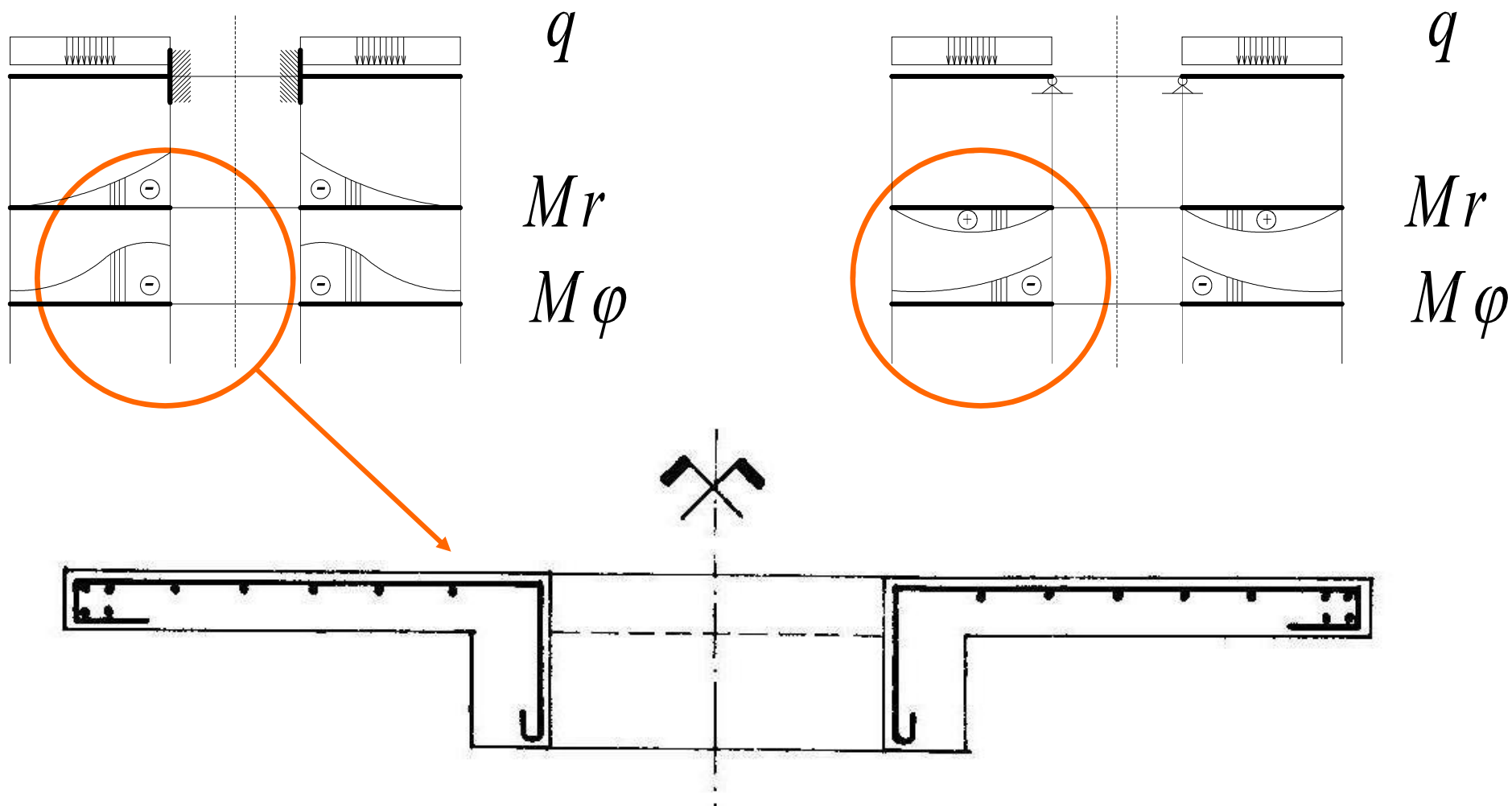
I varijanta



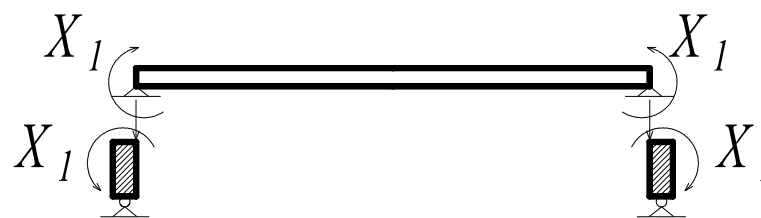
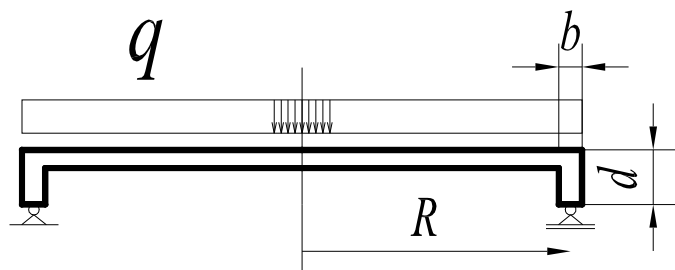
II varijanta



# Armiranje prstenastih ploča oslonjenih duž unutrašnje ivice



## Kružna ploča monolitno vezana sa kružnom gredom



$$X_1 \delta_{11} + \delta_{1p} = 0$$

$\delta_{11}$  - zajednički ugao obrtanja oslonačkog preseka i ploče u osnovnom sistemu pri delovanju  $X_1=1$

$$\delta_{11} = \varphi_{plo} + \varphi_{prs}$$

$\delta_{1p}$  - ugao obrtanja oslonačkog preseka u osnovnom sistemu od spoljašnjeg opterećenja

$$\varphi_{plo} = \frac{X_1 R}{EI_{plo}}$$

$$\varphi_{prs} = \frac{X_1 R^2}{EI_{prs}}$$

$$I_{plo} = \frac{d_p^3}{12}$$

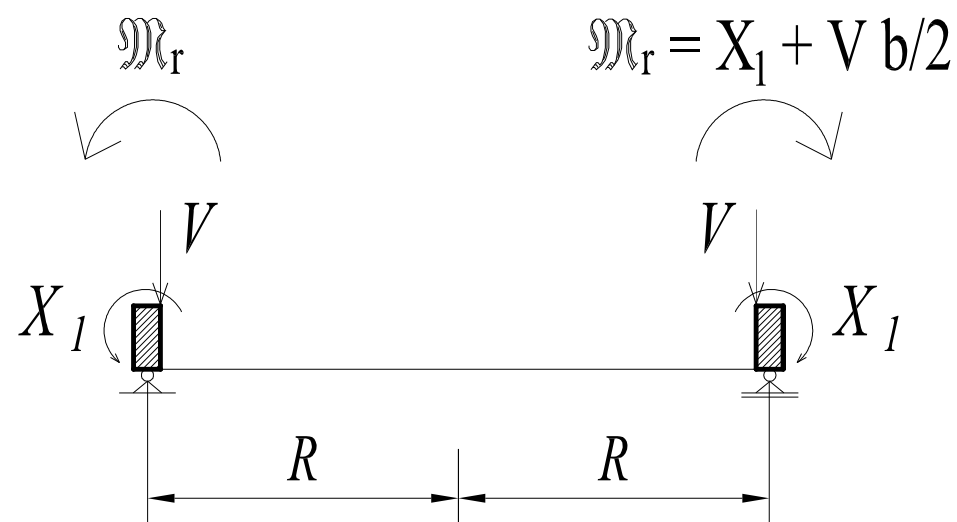
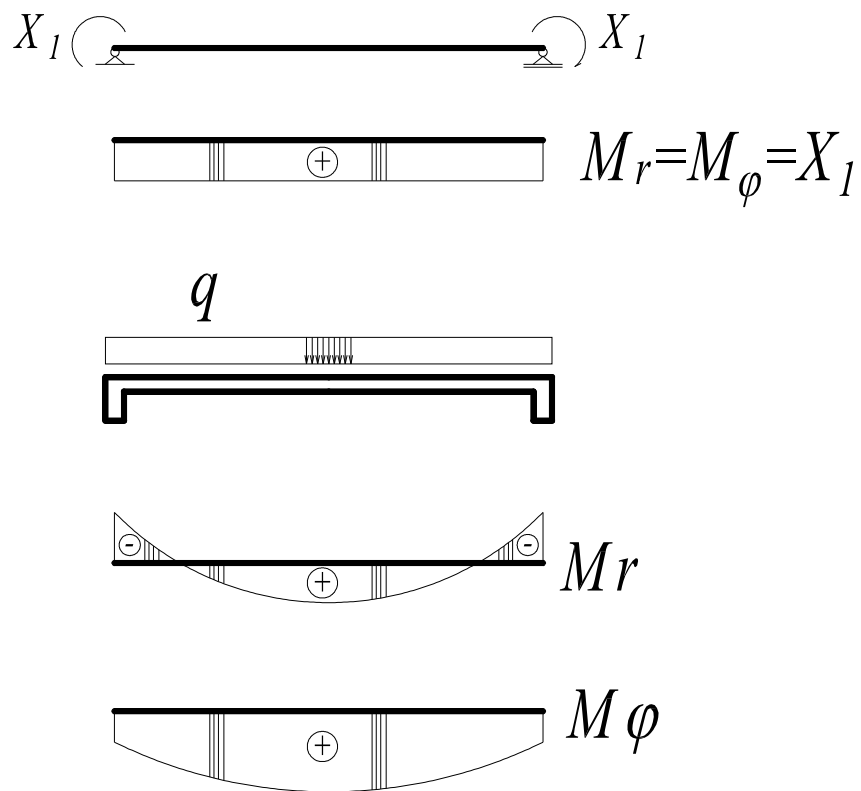
$$I_{prs} = \frac{bd^3}{12}$$

$$\delta_{1p} = 0.125 \frac{q \cdot R^3}{EI_{plo}}$$

## Moment savijanja u ploči

$$M_r = X_1 + M_r^q$$

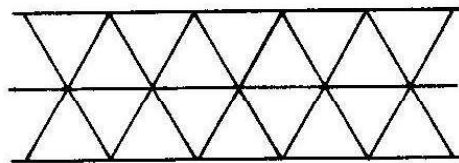
$M_r^q$  - radijalni moment u ploči u osnovnom sistemu



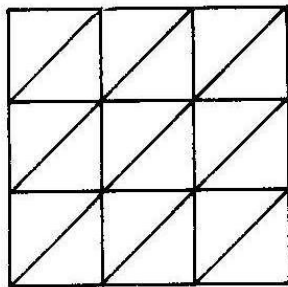
$$M_{\text{savijana prstena}} = \mathfrak{M}_r R$$

# Trougaone i trapezne ploče

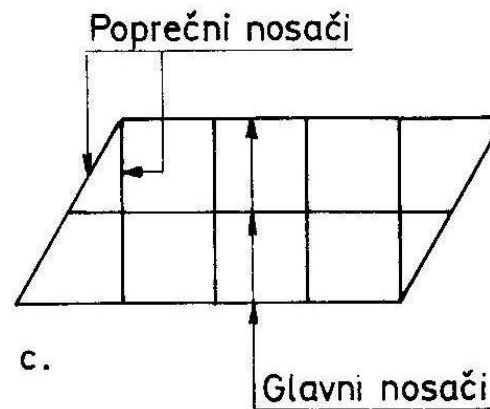
Ove ploče se javljaju kod međuspratnih konstrukcija kod kojih se grede, na koje se oslanjaju ploče, seku pod uglom – najčešće je to ugao od  $60^\circ$  – tako da grede formiraju trougaoni raster. Trougaone ploče su vrlo ekonomične jer je njihov statički rad vrlo racionalan, tako da se u njima javljaju relativno mali momenti savijanja. Mogu biti pojedinačne ploče, ili kontinualne.



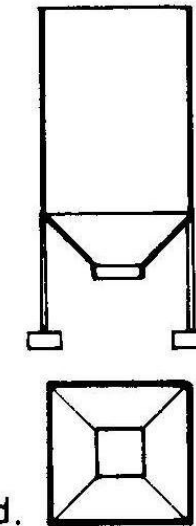
a.



b.



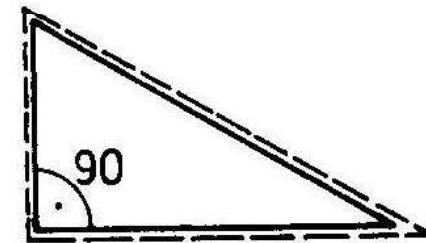
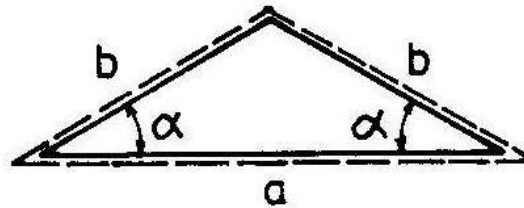
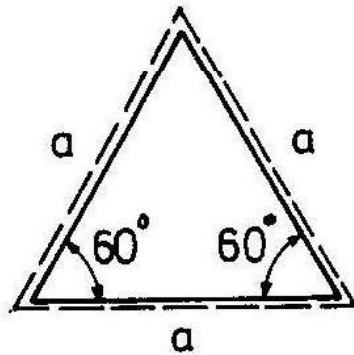
c.



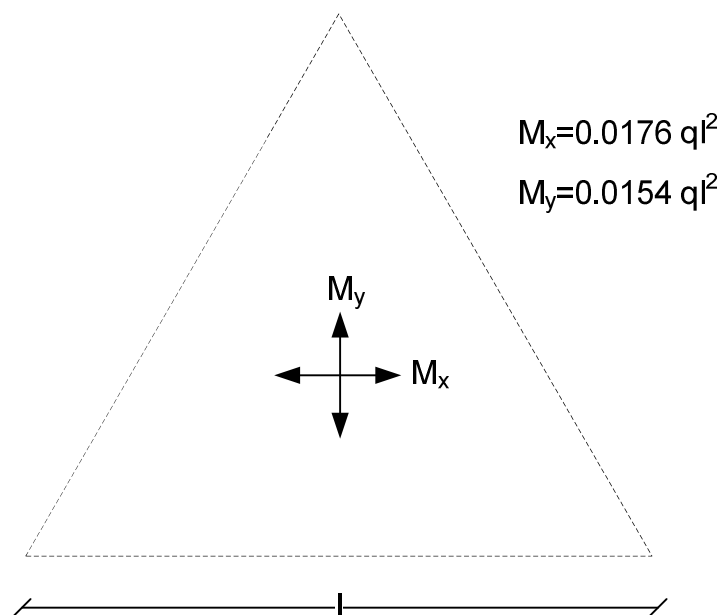
d.

# Pojedinačne trougaone ploče

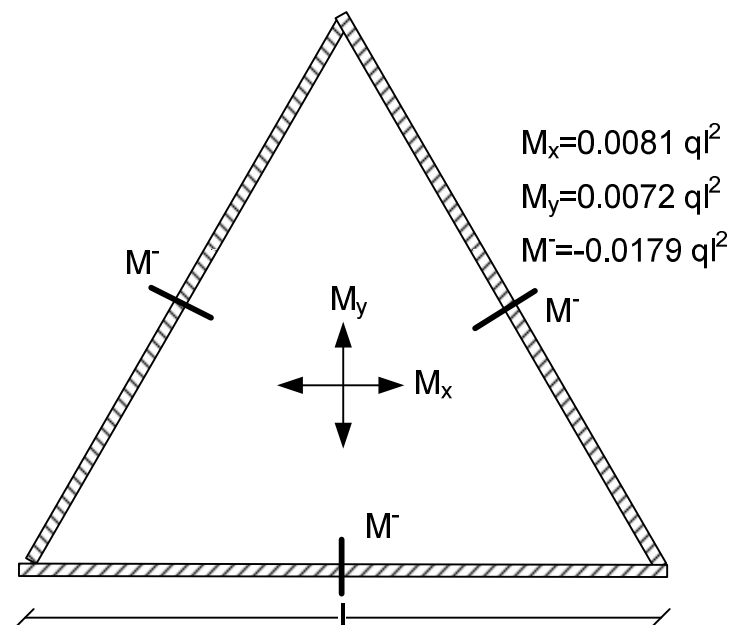
Pojedinačne trougaone ploče se najčešće projektuju kao jednakostranični trouglovi sa unutrašnjim uglovima od  $60^\circ$ , ali mogu biti i u obliku pravouglih ili raznokrakah trouglova:



Konturni uslovi su: slobodno linijsko oslanjanje duž pojedinih stranica, puno uklještenje, ili elastično uklještenje pojedinih stranica .

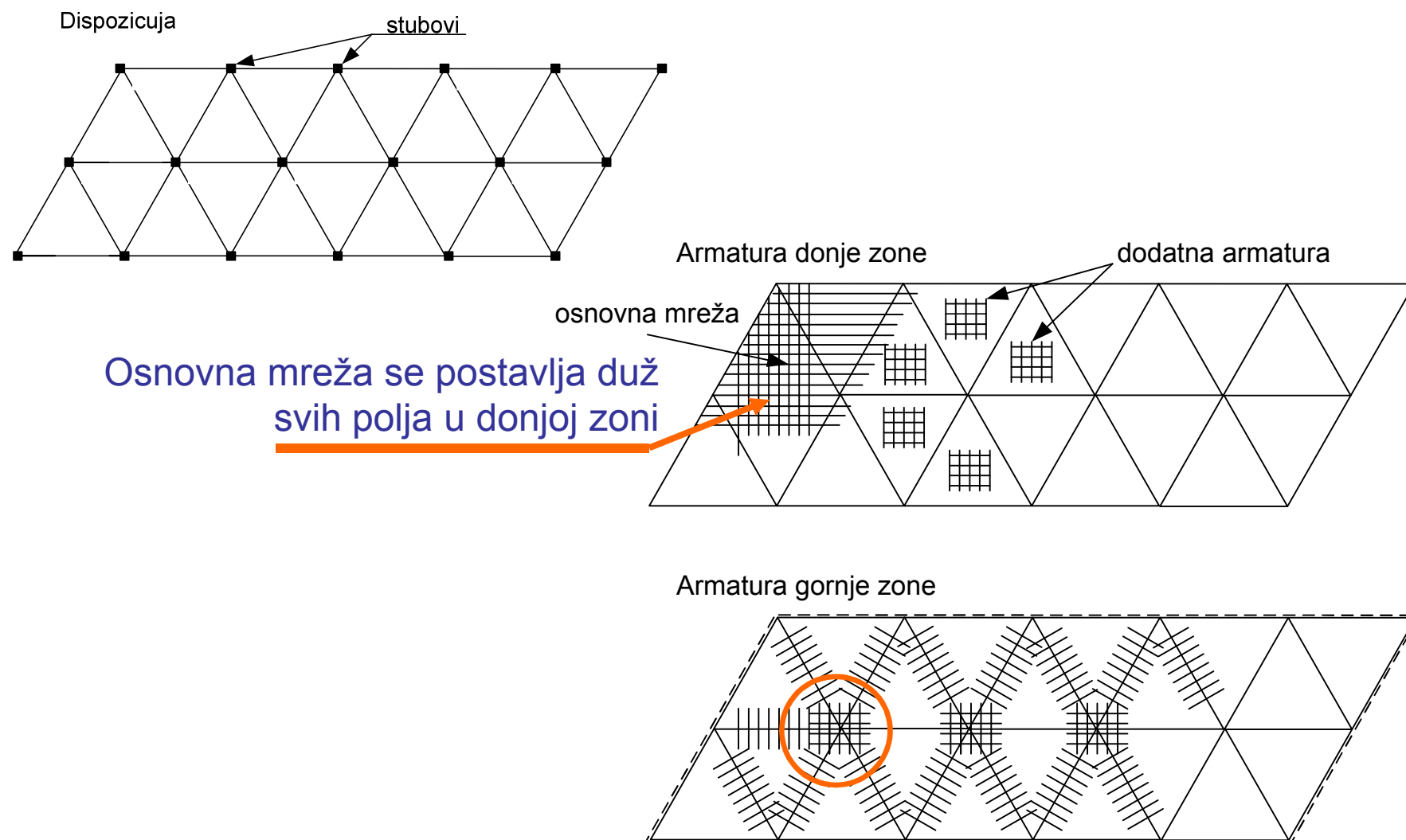


slobodno linijsko oslanjanje



puno uklještenje

# Armiranje kontinualnih trougaonih ploča

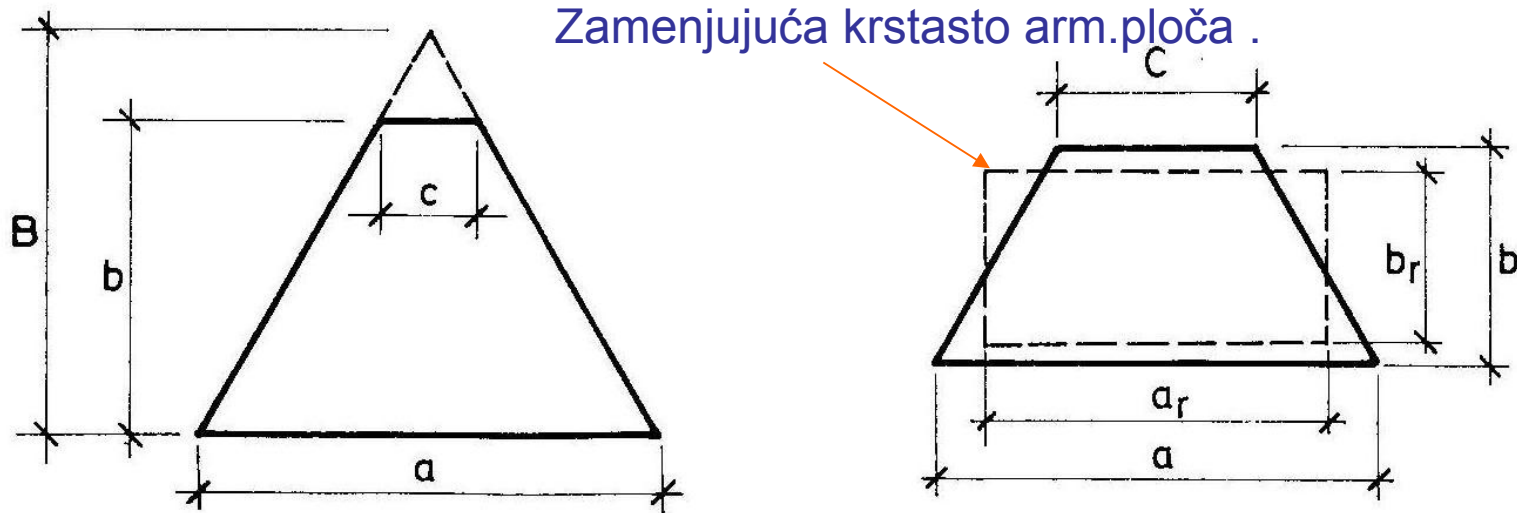


# Trapezne ploče

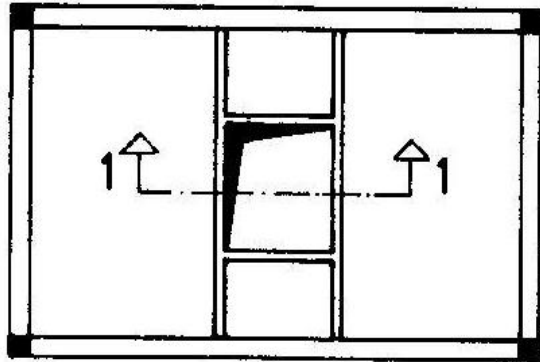
Trapezne ploče se ponašaju slično kao krstasto armirane ili trougaone ploče, pa se tako i proračunavaju i armiraju. Za praktičnu upotrebu ove ploče dovoljno tačno se mogu tretirati kao pravougaone krstasto armirane ploče kada je  $c/a > 0.25$ . U tom slučaju treba redukovati dužine stranica prema sledećim izrazima:

$$a_r = \frac{2}{3}(2c+a)a/(a+c) \text{ i } b_r = b - a(a-c)/(b(a+c))$$

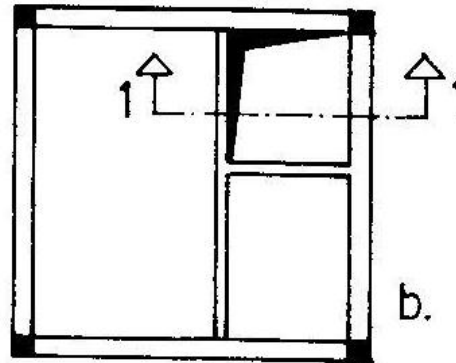
Kada je  $c/a \leq 0.25$  trapezne ploče se analiziraju kao trougaone ploče sa visinom  $B = ba/(a-c)$



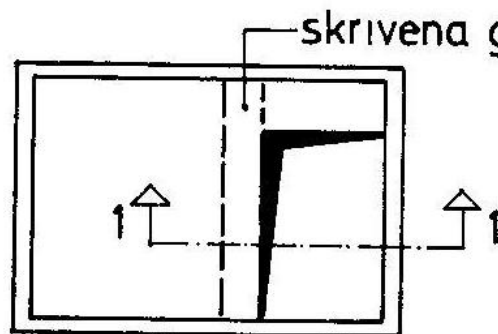
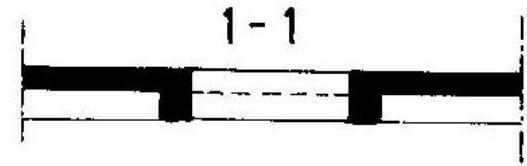
# Otvori u pločama



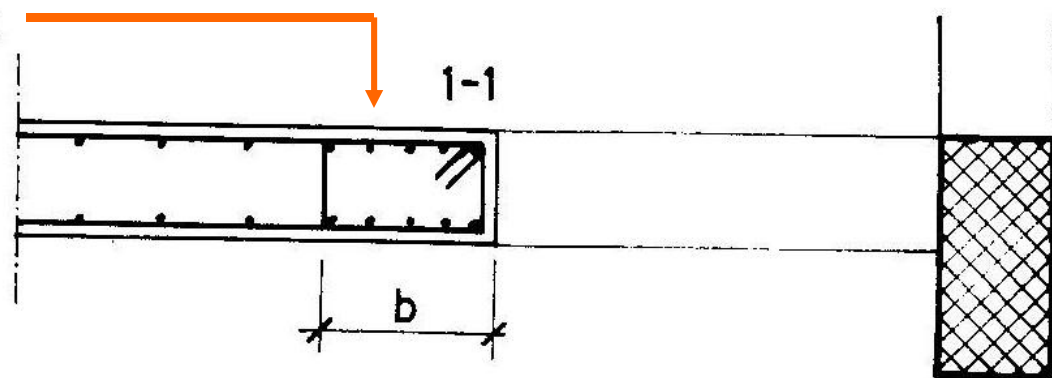
a.



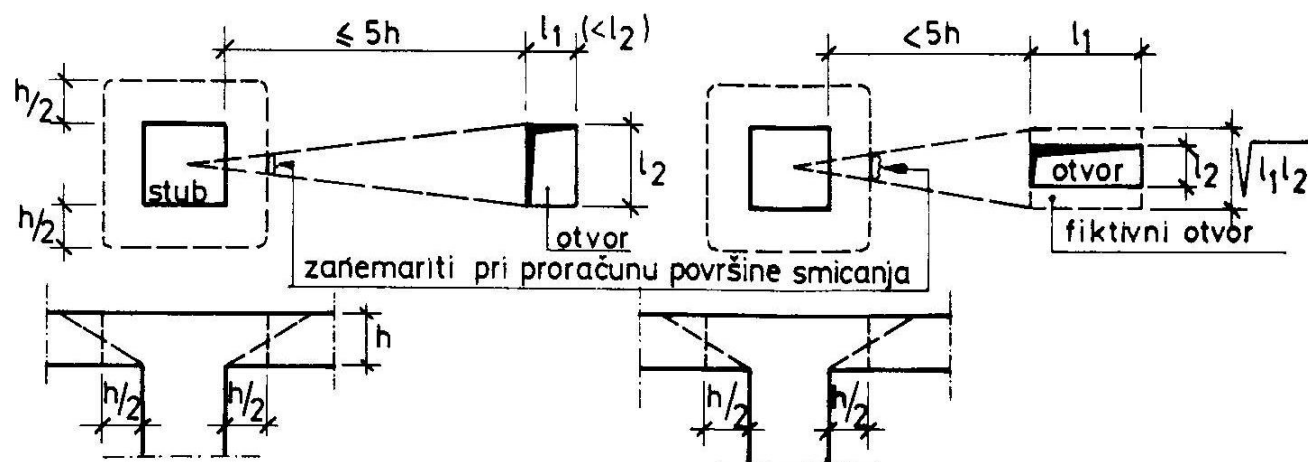
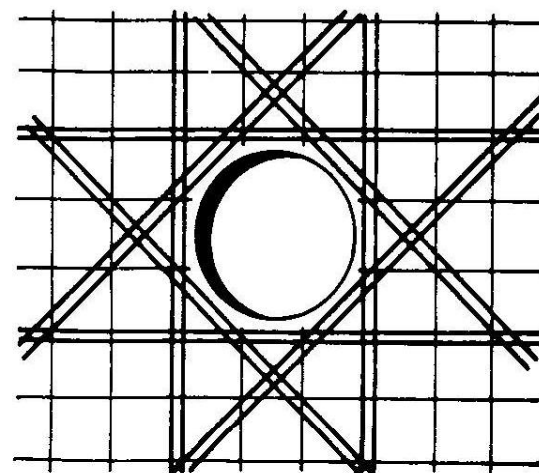
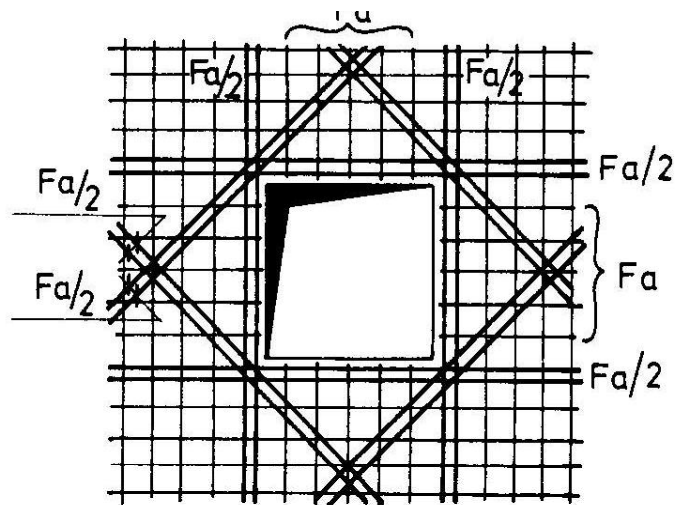
b.



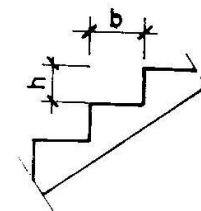
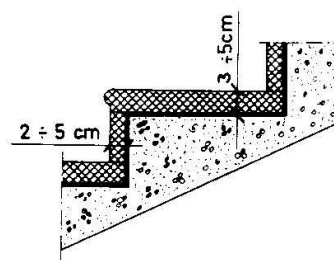
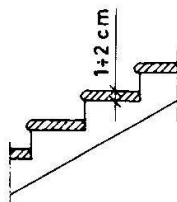
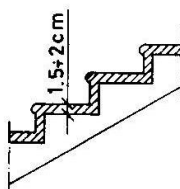
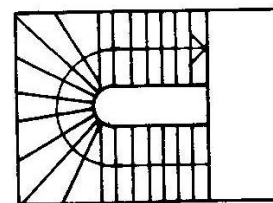
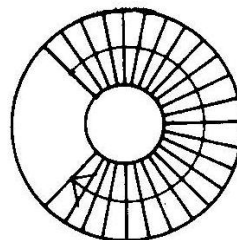
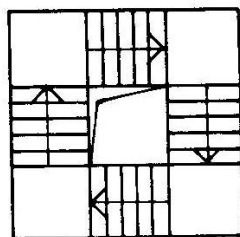
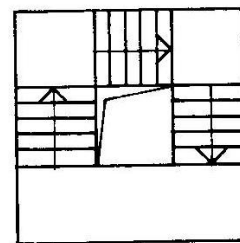
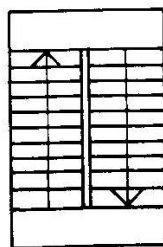
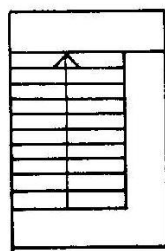
skrivena greda



# Armiranje otvora

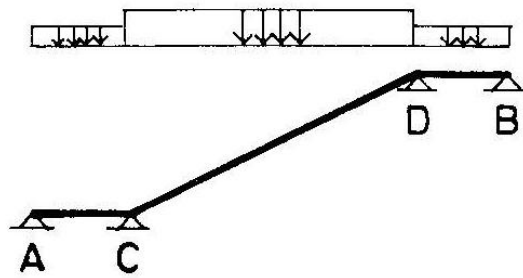
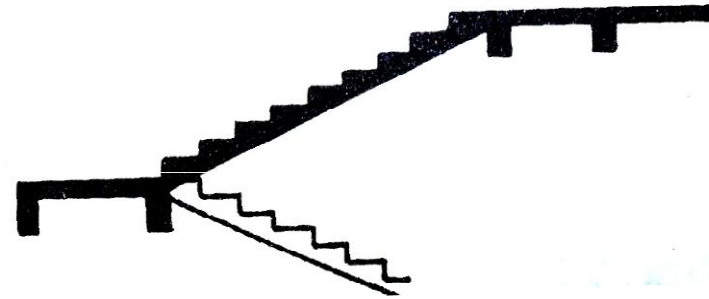
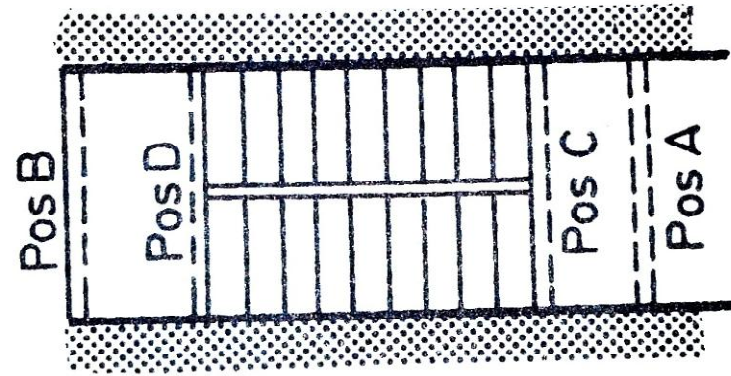


# Stepeništa

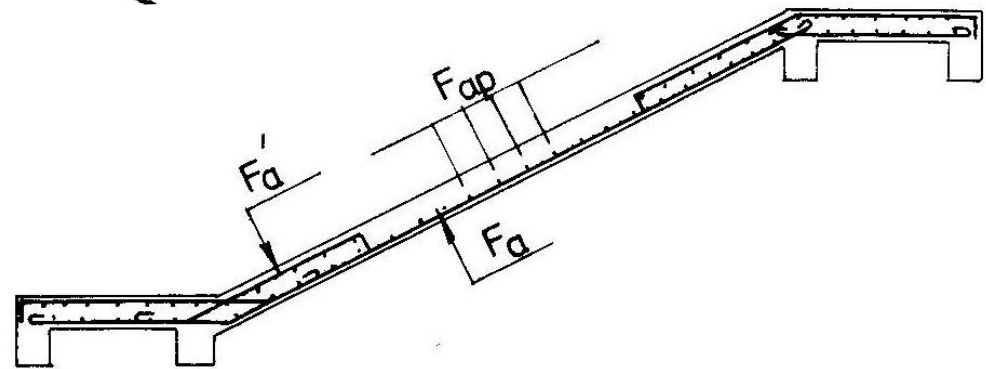


$$b + 2h = 63 \text{ cm}$$

$$b + h = 46 \text{ cm}$$



a)

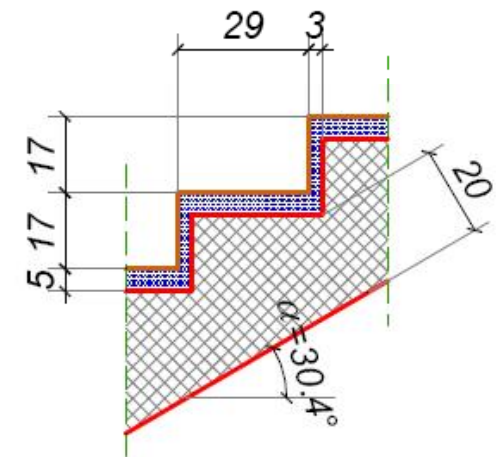
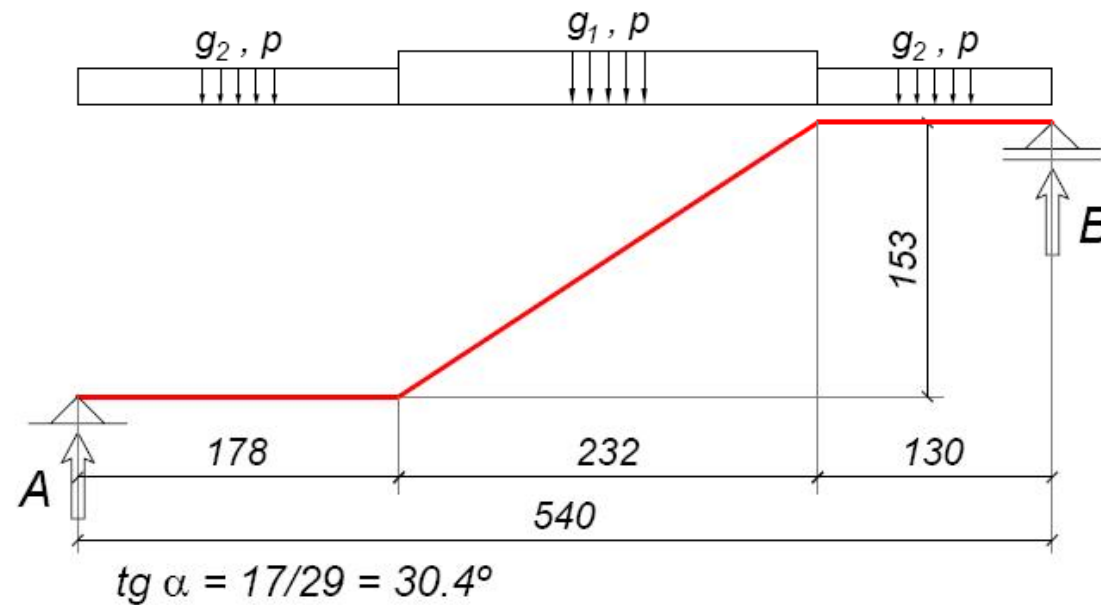


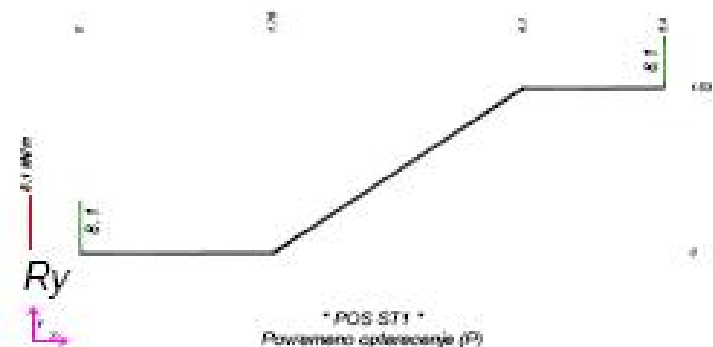
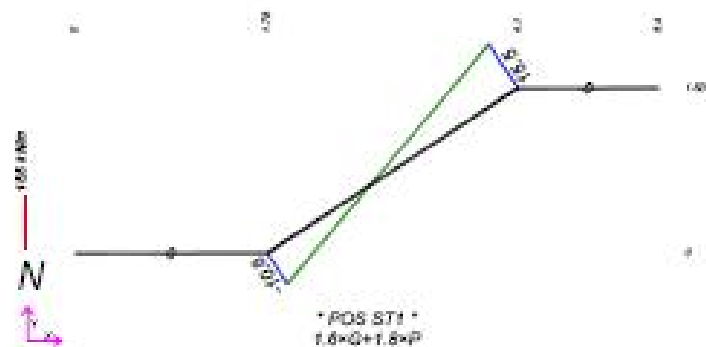
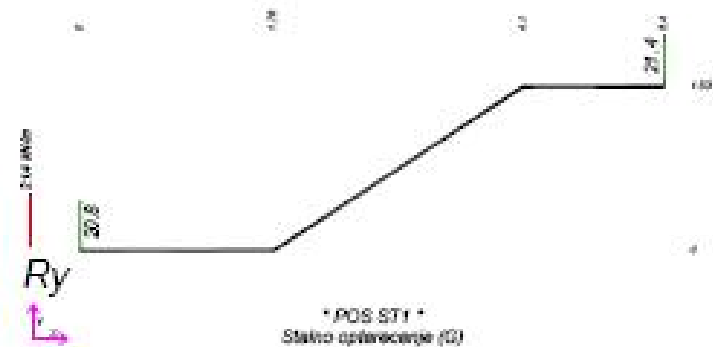
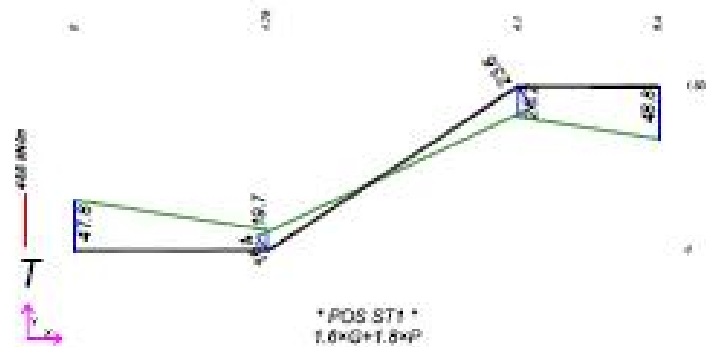
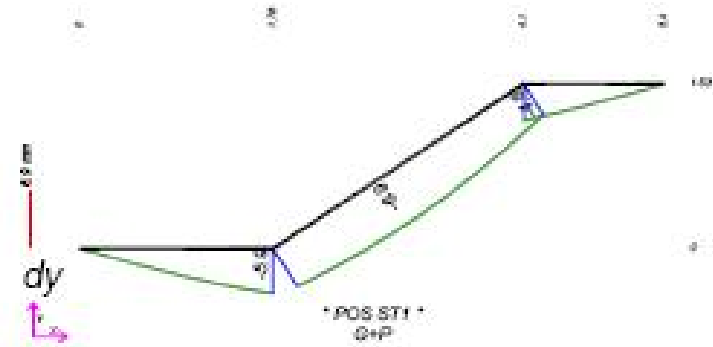
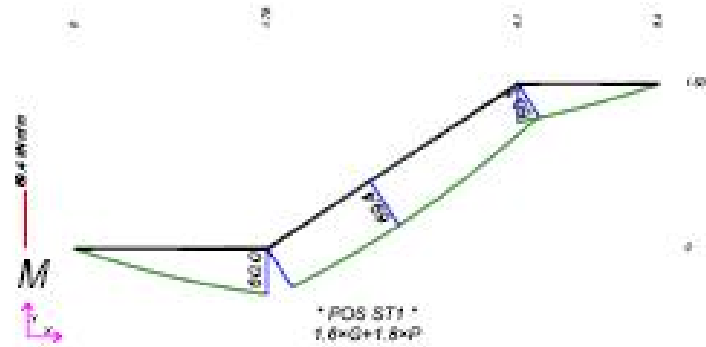
b)

## PRORAČUN STEPENIŠTA

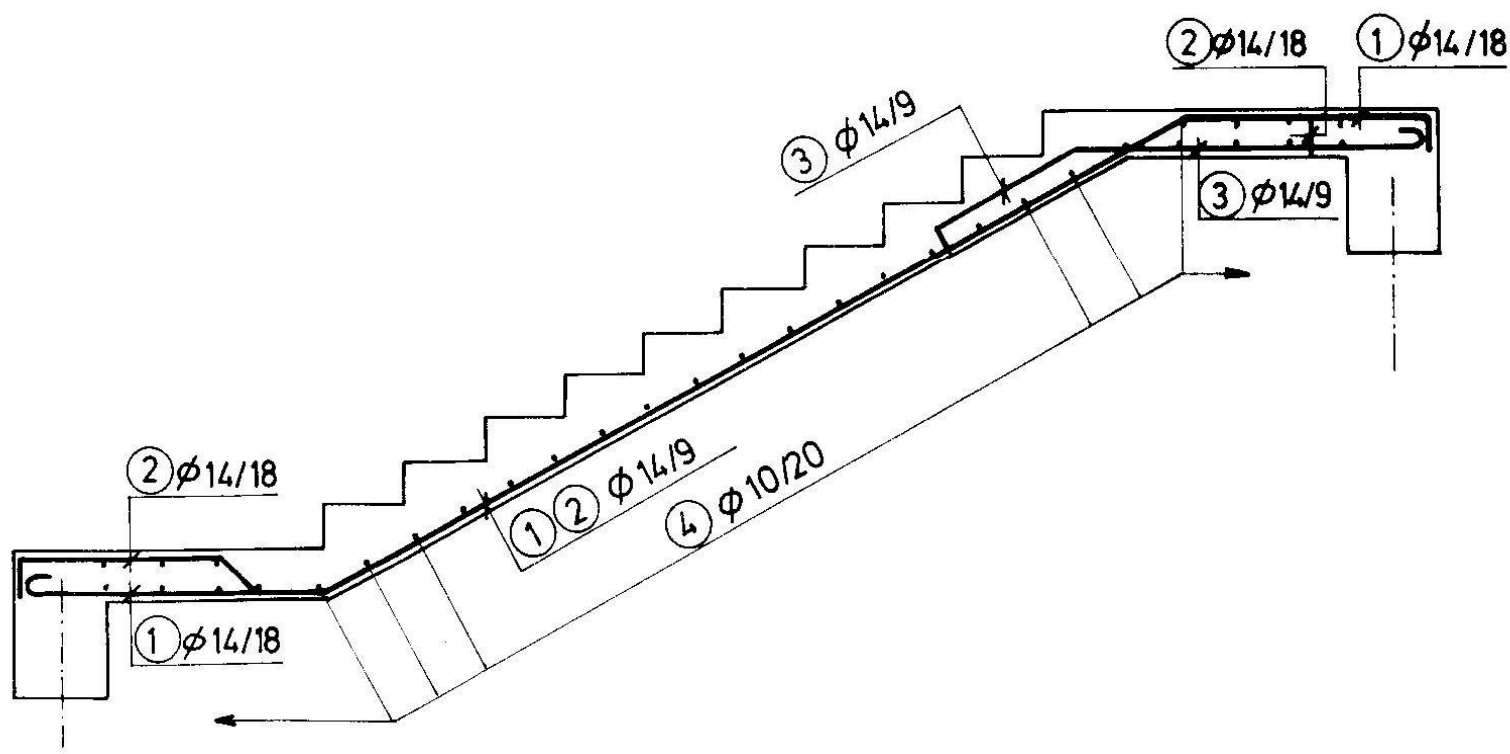
### POS ST1

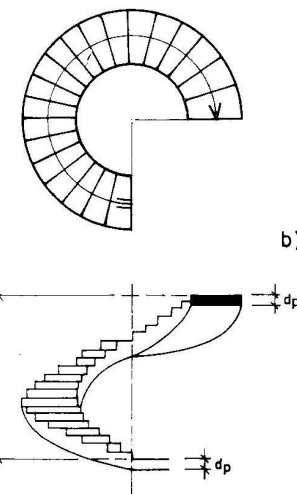
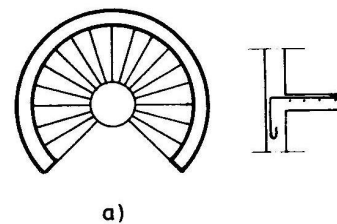
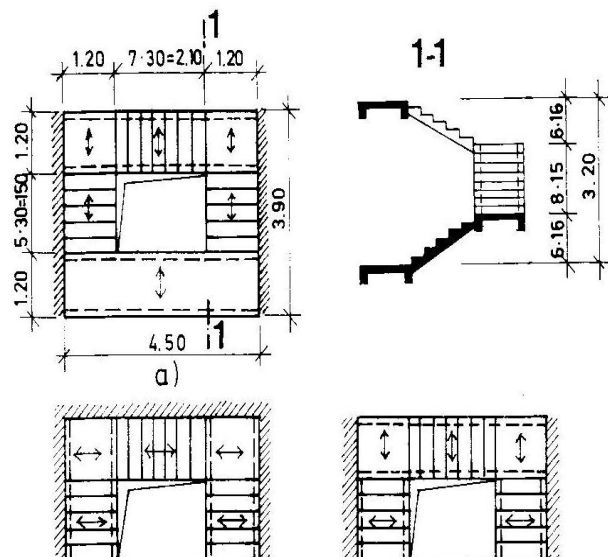
Stepenište je statičkog sistema kolenaste ploče, debljine  $d_p = 20$  cm. Savladava visinsku razliku od 306 cm između prizemlja i sprata (18 visina po 17 cm). Stepenci su dimenzija 17/29 cm. Debljina vertikalne obloge stepenika je 3 cm, a horizontalne 5 cm.



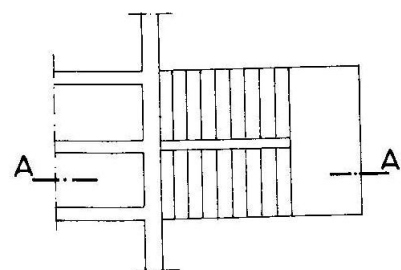


## Armiranje stepenišnog kraka

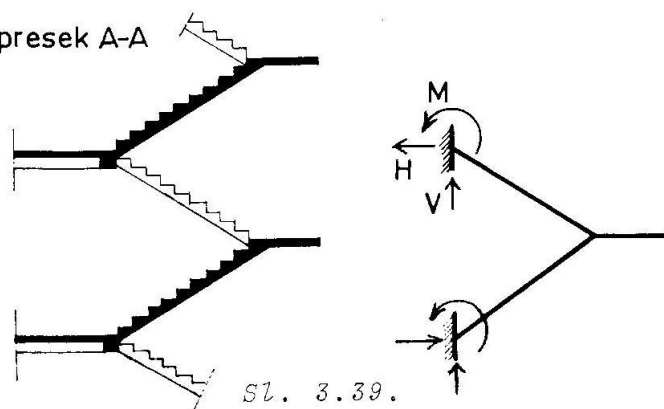




Sl. 3.37.



presek A-A



Sl. 3.39.

